

## LIST OF SYMBOLS AND NOTATIONS

|                     |  |
|---------------------|--|
| $\alpha$            | The effect of elasticity   |
| $\beta$             | The hysteretic shape parameter   |
| $\delta$            | Portion of error correction weight adjustment for $w_j$ that is due to an error at output unit $O$ ; also, the information about their error at unit $O$ that is propagated back to the hidden units that feed into unit $O$ |
| $\delta_h$          | Portion of error correction weight adjustment for $u_{ih}$ that is due to the backpropagation of error information from the output layer to the hidden unit $Z_h$  |
| $\delta_j$          | Portion of error correction weight adjustment for $v_{hj}$ that is due to the backpropagation of error information from the output layer to the hidden unit $K_j$  |
| $\varepsilon$       | Hysteretic energy dissipation  |
| $\gamma$            | The hysteretic shape parameter   |
| $\eta(\varepsilon)$ | The stiffness degradation parameter  |
| $\lambda$           | Pinching parameter   |
| $\mu$               | Learning rate  |
| $v_{hj}$            | Weight from hidden unit $Z_h$ to hidden unit $K_j$   |
| $v_{hj,n}$          | Update weight unit $hj$  |
| $v_{hj,o}$          | Old weight unit $hj$   |
| $v_{oj}$            | Bias on hidden unit $j$  |
| $\psi_0$            | Pinching parameter   |
| $\Theta$            | Performance Index  |
| $A$                 | Slope of CJ hysteretic model   |
| $A_{g1}$            | First generated KT seismic record  |
| $A_{g2}$            | Second generated KT seismic record   |
| $A_g$               | Ground Acceleration Record   |
| $ANN$               | Functional form of ANN   |
| $c$                 | Y axis-interception  |
| $c$                 | Damping  |
| $c$                 | Damping matrix   |
| $d$                 | Constant parameter control pinching behavior   |
| $D$                 | The accumulated plastic deformation of the CJ hysteretic element   |
| $D_o$               | Damage at time step $t_0$  |
| $e$                 | Residual between target and output   |
| $E$                 | Error Criterion / Objective Function   |
| $ETOL$              | Energy tolerance   |
| $f(x)$              | Activation Function  |
| $f_{ANN}$           | Predicting Restoring / Spring Force by ANNs  |
| $f_c$               | Damping Force  |
| $f_s$               | Spring Force   |
| $f_R$               | Restoring Force  |
| $f_{ANN}$           | Predicting Restoring / Spring Force vector   |
| $f_s$               | Spring force vector  |
| $g(t)$              | A temporal modulation function   |
| $h$                 | Index number of hidden layer 1 neuron  |
| $H(x)$              | Unit step function   |

|                             |   |
|-----------------------------|---|
| $i$                         | Index number of input neuron  |
| $j$                         | Index number of hidden layer 2 neuron                               |
| $k$                         | K-iteration of implicit time integration                            |
| $k_1$                       | Linear stiffness  |
| $k_2$                       | Nonlinear stiffness   |
| $k_j$                       | Output value unit $K_j$   |
| $k_{in_j}$                  | Summation value of weight input signal unit $j$                     |
| $K_j$                       | Hidden unit $j$   |
| $l$                         | Number of training data set   |
| $m$                         | Slope of linear equation  |
| $m$                         | Mass  |
| $\mathbf{m}$                | Mass matrix   |
| $n$                         | Number of input neuron  |
| $n_u$                       | Numbers of time steps of displacement                               |
| $n_v$                       | Numbers of time steps of velocity                                   |
| $n_f$                       | Numbers of time steps of restoring / spring force                   |
| $o$                         | Resulting output value computing by ANNs                            |
| $o_{in}$                    | Summation value of weight input signal output unit                  |
| $O$                         | Output Neuron   |
| $p$                         | Number of neuron in hidden layer 2                                  |
| $P_{ext}$                   | External Force  |
| $q$                         | Number of neuron in hidden layer 1                                  |
| $r$                         | EBWBN hysteretic parameter  |
| $RTOL$                      | Force tolerance   |
| $s$                         | A parameter controlling the rate of initial drop in slope           |
| $SREE$                      | Sum Square Relative Error   |
| $t$                         | Time step $t$   |
| $t$                         | Target value  |
| $\Delta t$                  | Increment time step $\Delta t$                                      |
| $u$                         | Displacement  |
| $\dot{u}$                   | Velocity  |
| $\ddot{u}$                  | Acceleration  |
| $u_o$                       | Displacement at time step $t_0$                                     |
| $\dot{u}_o$                 | Velocity at time step $t_0$   |
| $\ddot{u}_o$                | Acceleration at time step $t_0$                                     |
| $u_{oh}$                    | Bias on hidden unit $h$   |
| $u_{ih}$                    | Weight from input unit $y_i$ to hidden unit $Z_h$                   |
| $u_{ih,n}$                  | Update weight unit $ih$   |
| $u_{ih,o}$                  | Old weight unit $ih$  |
| $u_{ih}^*, v_{hj}^*, w_j^*$ | The optimal weights that derived from training procedure            |
| $\Delta u_{ih}$             | Weight adjustment value from input unit $y_i$ to hidden unit $Z_h$  |
| $v(\varepsilon)$            | The strength degradation parameter                                  |
| $\Delta v_{hj}$             | Weight adjustment value from hidden unit $Z_h$ to hidden unit $K_j$ |
| $w_j$                       | Weight from hidden unit $K_j$ to output unit $O$                    |
| $w_o$                       | Bias on output unit   |
| $\Delta w_j$                | Weight adjustment value from hidden unit $K_j$ to output unit $O$   |
| $w_{j,n}$                   | Update weight unit $j$  |
| $w_{j,o}$                   | Old weight unit $j$   |

|              |  |
|--------------|--|
| $W(t)$       | A stationary Gaussian white noise process with 2-side power spectral $G_0$ |
| $x$          | Original /raw input or output value  |
| $x$          | Relative displacement  |
| $X_{\min}$   | Minimum of input or output value   |
| $y$          | Scale input or output value  |
| $\mathbf{y}$ | Input vector to ANNs   |
| $y_i$        | Input to network node $i$  |
| $Z_Y$        | The yield level  |
| $Z$          | The hysteretic displacement of CJ hysteretic system                        |
| $z_h$        | Output value unit $Z_h$  |
| $Z_h$        | Hidden unit $h$  |
| $z\_in_h$    | Summation value of weight input signal unit $h$                            |